SECTION A – Multiple-choice questions

Instructions for Section A

cation Answer all questions in pencil on the answer sheet provided for multiple-choice questions.

Choose the response that is correct for the question.

A correct answer scores 1; an incorrect answer scores 0.

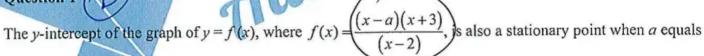
Marks will not be deducted for incorrect answers.

No marks will be given if more than one answer is completed for any question.

Unless otherwise indicated, the diagrams in this book are not drawn to scale

Take the acceleration due to gravity to have magnitude g ms⁻², where g = 9.8

Question 1



B.
$$-\frac{6}{5}$$

$$f'(0) = 0$$

Solve $\left(\frac{d}{dx}(\sqrt{x}) = 0, a\right)|x = 0$

$$\boxed{\mathbf{D}.} \quad \frac{6}{5}$$

Question 2



A function f has the rule $f(x) = |b\cos^{-1}(x) - a|$, where a > 0, b > 0 and $a < \frac{b\pi}{2}$.

The range of f is

B.
$$[0, b\pi - a]$$

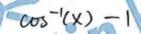
C.
$$[a, b\pi - a]$$

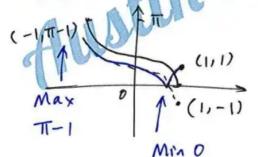
D.
$$[0, b\pi + a]$$

acbu

$$\cos^{-1}(x) = \frac{a}{b}$$

$$x = cos(\frac{a}{b})$$





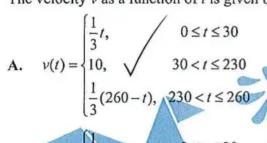
ducation



A train is travelling from Station A to Station B. The train starts from rest at Station A and travels with constant acceleration for 30 seconds until it reaches a velocity of 10 ms⁻¹. It then travels at this velocity for 200 seconds. The train then slows down, with constant acceleration, and stops at Station B having travelled for 260 seconds in total. Let v ms⁻¹ be the velocity of the train at time t seconds.

3

The velocity v as a function of t is given by





B.
$$v(t) = 10$$
, $30 < t \le 250$
 $\frac{1}{3}(230 - t)$, $230 < t \le 260$

C.
$$v(t) = \begin{cases} 3t, & 0 \le t \le 30 \\ 10, & 30 < t \le 230 \\ 3(230 - t), & 230 < t \le 260 \end{cases}$$

$$\mathbf{D.} \quad \nu(t) = \begin{cases} 3t, & 0 \le t \le 30 \\ 10, & 30 < t \le 230 \\ 3(260 - t), & 230 < t \le 260 \end{cases}$$

$$\mathbf{E.} \quad v(t) = \begin{cases} \frac{1}{3}t, & 0 \le t \le 30\\ 10, & 30 < t \le 200\\ \frac{1}{3}(230 - t), & 200 < t \le 230 \end{cases}$$

$$\left(\frac{1}{3}(230-t),\right)$$

Question 4 Let $f(x) = \frac{\sqrt{x-1}}{x}$ over its implied domain and $g(x) = \csc^2 x$ for $0 < x < \frac{\pi}{2}$

The rule for f(g(x)) and the range, respectively, are given by

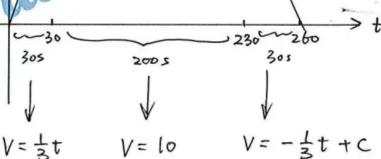
A.
$$f(g(x)) = \csc^2\left(\frac{\sqrt{x-1}}{x}\right), [1, \infty)$$

B.
$$f(g(x)) = \csc^2\left(\frac{\sqrt{x-1}}{x}\right), [2, \infty)$$

C.
$$f(g(x)) = \sin(x)\cos(x), [-0.5, 0.5] \setminus \{0\}$$

D.
$$f(g(x)) = \sin(x)\cos(x), (0, \frac{1}{2})$$

(E.)
$$f(g(x)) = \frac{1}{2}\sin(2x), \left(0, \frac{1}{2}\right)$$



$$\frac{230}{3} + C = 10$$

$$C = \frac{2bv}{3}$$

$$V = -\frac{1}{3}(t - 260)$$

$$V = \frac{1}{3}(260-t)$$

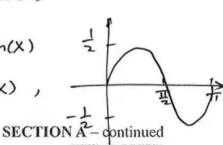
$$(g(x)) = \sqrt{csc^2(x)} - 1$$
 $csc^2(x)$

$$\frac{\cot(x)}{\csc^2(x)}$$

$$= \frac{\cos(x)}{\sin(x)} \sin^2(x)$$

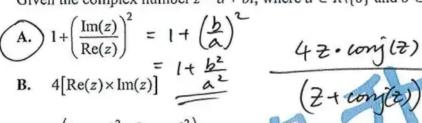
$$= \cos(x)\sin(x)$$

$$= \int \sin(2x),$$





Given the complex number z = a + bi, where $a \in R \setminus \{0\}$ and $b \in R$, $\frac{4z\overline{z}}{(z+\overline{z})^2}$ is equivalent to



$$\mathbb{R}$$
 \mathbb{R} \mathbb{R} \mathbb{R}

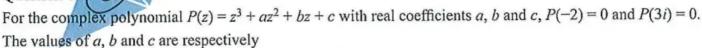
C.
$$4([Re(z)]^2 + [Im(z)]^2)$$

D.
$$4 \left[1 + \left(\text{Re}(z) + \text{Im}(z) \right)^2 \right]$$

$$E_{x} = \frac{2 \times Im(z)}{2}$$



Question 6/6

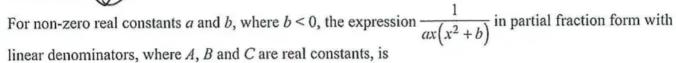


A.
$$-2, 9, -18$$

E.
$$2, -9, -18$$

expand((Z+2)(2-3i)(2+3i))

Question 7 (D



A.
$$\frac{A}{ax} + \frac{Bx + C}{x^2 + b}$$

B.
$$\frac{A}{ax} + \frac{B}{x + \sqrt{b}} + \frac{C}{x - \sqrt{b}}$$

C.
$$\frac{A}{x} + \frac{B}{ax + \sqrt{|b|}} + \frac{C}{ax - \sqrt{|b|}}$$

$$\underbrace{\mathbf{D.}} \quad \frac{A}{x} + \frac{B}{x + \sqrt{|b|}} + \frac{C}{x - \sqrt{|b|}}$$

E.
$$\frac{A}{ax} + \frac{B}{\left(x + \sqrt{b}\right)^2} + \frac{C}{x + \sqrt{b}}$$

expand
$$(\frac{1}{a \cdot x \cdot (x^2 + b)}, x)/b < 0$$

-a - ib

b - ia

C. -b + ia

-a + ib

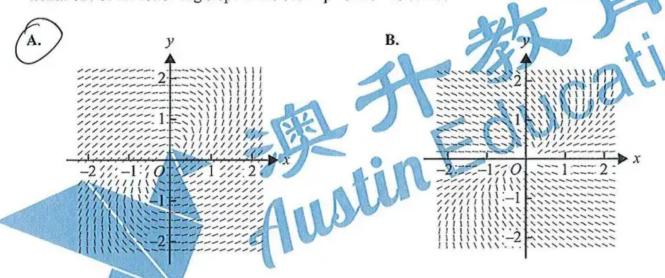
E. b + ia

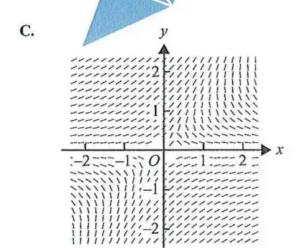
Given that $(x+iy)^{14} = a+ib$, where $x, y, a, b \in R$, $(y-ix)^{14}$ for all values of x and y is equal to (y-ix) = (i(-x-yi = (- i (x+yi)



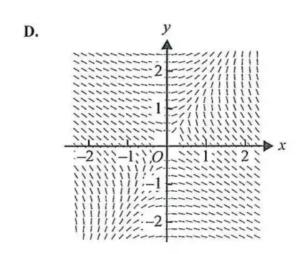
Question 9 7

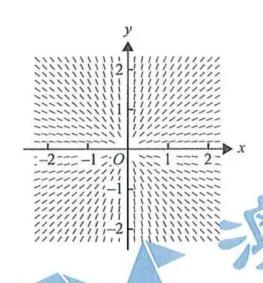
P(x, y) is a point on a curve. The x-intercept of a tangent to point P(x, y) is equal to the y-value at P. Which one of the following slope fields best represents this curve?





E.





$$\frac{dy}{dx}\Big|_{x=x_0}$$

$$y - y_0 = \left(\frac{dy}{dx}\right)(x - x_0)$$

$$x - int: y = 0$$

$$y_0 = \frac{\partial y}{\partial x} (x - x_0)$$

$$x = x_0 - \frac{y_0}{\left(\frac{\partial y}{\partial x}\right)}$$

y = int: x = 0 $y = \frac{ony}{2}$

ly ay

$$\frac{\partial y}{\partial x} \left(\frac{x_0}{y_0} \right) = x_0 - \frac{y_0}{\partial y}$$

SECTION A - continued



A tank initially contains 300 grams of salt that is dissolved in 50 L of water. A solution containing 15 grams of salt per litre of water is poured into the tank at a rate of 2 L per minute and the mixture in the tank is kept well stirred. At the same time, 5 L of the mixture flows out of the tank per minute.

Well stirred. At the same time, 3 L of the mixture flows out of the tank per minute.

A differential equation representing the mass, m grams, of salt in the tank at time t minutes, for a non-zero volume of mixture, is

A. $\frac{dm}{dt} = 0$ B. $\frac{dm}{dt} = -\frac{5m}{50-5t}$ C. $\frac{dm}{dt} = 30 - \frac{m}{10}$ D. $\frac{dm}{dt} = 30 - \frac{5m}{50-3t}$

A.
$$\frac{dm}{dt} = 0$$

B.
$$\frac{dm}{dt} = -\frac{5m}{50 - 5t}$$

C.
$$\frac{dm}{dt} = 30 - \frac{m}{10}$$

$$\boxed{\mathbf{D.}} \frac{dm}{dt} = 30 - \frac{5m}{50 - 3t}$$

$$E. \quad \frac{dm}{dt} = 30 - \frac{5m}{50 - 5t}$$





Question 11 C Suproper integral

With a suitable substitution $\int_{-\frac{\pi}{4}}^{\frac{\pi}{3}} \frac{\sec^2(x)}{\sec^2(x) - 3\tan(x) + 1} dx \text{ can be expressed as}$ $\mathcal{U} = \tan(\mathcal{X})$

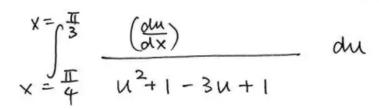
A.
$$\int_{1}^{\frac{1}{\sqrt{3}}} \left(\frac{1}{u-1} - \frac{1}{u-2} \right) du$$

B.
$$\int_{1}^{\sqrt{3}} \left(\frac{1}{3(u-3)} - \frac{1}{3u} \right) du$$

$$C. \int_{1}^{\sqrt{3}} \left(\frac{1}{u-2} - \frac{1}{u-1}\right) du$$

$$\mathbf{D.} \quad \int_{1}^{\sqrt{3}} \left(\frac{1}{u-1} - \frac{1}{u-2} \right) du$$

E.
$$\int_{\frac{\pi}{4}}^{\frac{\pi}{3}} \left(\frac{1}{3(u-1)} - \frac{1}{3(u+2)} \right) du$$



$$\rightarrow \int_{1}^{\sqrt{3}} \frac{1}{u^2 - 3u + 2} du$$

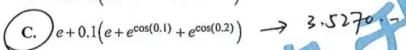






If $\frac{dy}{dx} = e^{\cos(x)}$ and $y_0 = e$ when $x_0 = 0$, then, using Euler's formula with step size 0.1, y_3 is equal to ducation

- $e+0.1\left(1+e^{\cos(0.1)}\right)$
- $e + 0.1(1 + e^{\cos(0.1)} + e^{\cos(0.2)})$ В.



D.
$$e + 0.1(e^{\cos(0.1)} + e^{\cos(0.2)} + e^{\cos(0.3)})$$

E.
$$e+0.1(e+e^{\cos(0.1)}+e^{\cos(0.2)}+e^{\cos(0.3)})$$

Question 13

+2 k and c = i + k will be **linearly dependent** when the value of λ is The vectors a = i

- 1
- 2
- 3
- 4 D.
- 5

Question 14



The magnitude of the component of the force $\mathbf{F} = \mathbf{j} + 6\mathbf{j} - 18\mathbf{k}$ that acts in the direction $\mathbf{d} = 2\mathbf{j} - 3\mathbf{j} - 6\mathbf{k}$ is

- $\frac{92}{19}$ A.
- - D.
 - E.



$$ZE = 6i + 3j = 3a \Rightarrow a = 2i + j^{2020 \text{ SPECMATH EXAM 2}}$$

Two forces, $F_A = 4i - 2j$ and $F_B = 2i + 5j$, act on a particle of mass 3 kg. The particle is initially at rest at position i + j. All force components are measured in newtons and displacements are measured in metres.

The cartesian equation of the path of the particle is

A.
$$y = \frac{x}{2}$$

B.
$$y = \frac{x}{2} - \frac{1}{2}$$

C.
$$y = \frac{(x+1)^2}{(x+1)^2} + 1$$

D.
$$y = \frac{(x-1)^2}{2} + 1$$

E.
$$y = \frac{x}{2} + \frac{1}{2}$$

Question 16

Let $\underline{a} = \underline{i} + 2\underline{j} + 2\underline{k}$ and $\underline{b} = 2\underline{i} - 4\underline{j} + 4\underline{k}$, where the acute angle between these vectors is θ .

The value of $\sin(2\theta)$ is

A.
$$\frac{1}{9}$$

B.
$$\frac{4\sqrt{5}}{9}$$

C.
$$\frac{4\sqrt{5}}{81}$$

$$\boxed{\mathbf{D}. \frac{8\sqrt{5}}{81}}$$

E.
$$\frac{2\sqrt{46}}{25}$$

Question 17

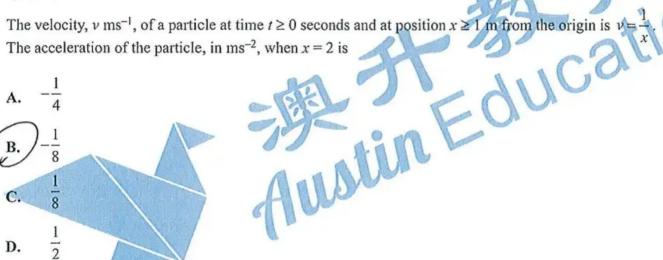
A.
$$-\frac{1}{4}$$

$$B$$
. $-\frac{1}{8}$

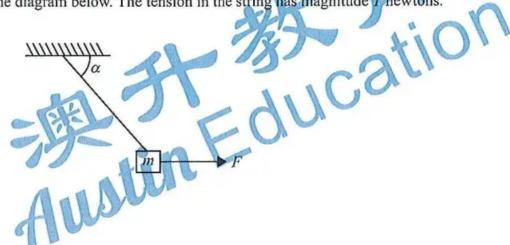
C.
$$\frac{1}{8}$$

D.
$$\frac{1}{2}$$

E.
$$\frac{1}{4}$$



A particle of mass m kilograms hangs from a string that is attached to a fixed point. The particle is acted on by a horizontal force of magnitude F newtons. The system is in equilibrium when the string makes an angle α to the horizontal, as shown in the diagram below. The tension in the string has magnitude T newtons.



The value of $tan(\alpha)$ is

- A. $\frac{mg}{T}$
- B. $\frac{T}{mg}$
- C. $\frac{T}{F}$
- $\mathbf{D.} \quad \frac{F}{mg}$



Question 19

A cricket ball of mass 0.02 kg, moving with velocity $2i - 10j \text{ ms}^{-1}$, is hit and after impact travels with velocity $2i - 7j \text{ ms}^{-1}$.

The magnitude of the change in momentum of the cricket ball, in kg ms-1, is closest to

- A. 0.04
- **B.** 0.06
- C. 0.10





Question 20

An object of mass 2 kg is suspended from a spring balance that is inside a lift travelling downwards.

If the reading on the spring balance is 30 N, the acceleration of the lift is



) 5.2 ms⁻² upwards.

- B. 5.2 ms⁻² downwards.
- C. 9.8 ms⁻² downwards.
- D. $10.4 \text{ ms}^{-2} \text{ upwards}$.
- E. 10.4 ms⁻² downwards.



2g - 30 = 2a

SECTION B

Instructions for Section B

Answer all questions in the spaces provided.

Unless otherwise specified, an exact answer is required to a question.

In questions where more than one mark is available, appropriate working must be shown.

Unless otherwise indicated, the diagrams in this book are not drawn to scale.

Take the acceleration due to gravity to have magnitude g ms⁻², where g = 9.8

Question 1 (12 marks)

A particle moves in the x-y plane such that its position in terms of x and y metres at t seconds is given by the parametric equations

$$x = 2\sin(2t)$$
$$y = 3\cos(t)$$

where $t \ge 0$

a. Find the distance, in metres, of the particle from the origin when $t = \frac{\pi}{6}$. CAS mark. 2 marks

Let $\Gamma(t) = \times \hat{L} + Y\hat{L}$

 $= \sqrt{39}$

b. i. Express $\frac{dy}{dx}$ in terms of t and, hence, find the equation of the tangent to the path of the

particle at $t = \pi$ seconds.

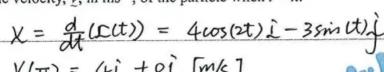
😘 marks

$$\frac{dy}{dx} = \frac{\frac{dy}{dt}}{\frac{dx}{dt}} = \frac{-3\sin(t)}{4\cos(xt)} \Rightarrow \frac{dy}{dt} = 0$$

That's a honizontal tangent

and the equ of tangent is y= - ?

Find the velocity, y, in ms⁻¹, of the particle when $t = \pi$.





$$X = \frac{d}{dt}(C(t)) = 4\cos(2t)\hat{L} - 3\sin(t)\hat{L}$$

$$X(\pi) = 4\hat{L} + 0\hat{L} [m/s]$$





$$\alpha = \frac{d}{dt}(x(t)) = -8\sin(2t)\hat{\lambda} - 3\cos(t)\hat{j}$$

$$\alpha(\pi) = 0\hat{\lambda} + 3\hat{j}$$

$$|\alpha(\pi)| = 3[m/s^{2}]$$

Find the time, in seconds, when the particle first passes through the origin.

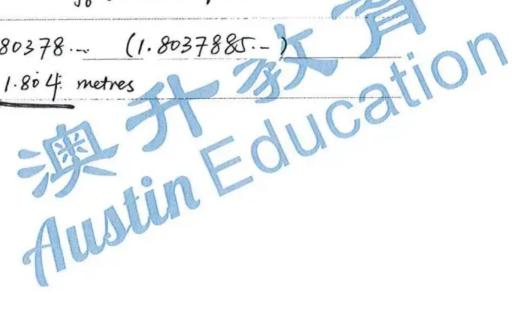
1 mark

Express the distance, d metres, travelled by the particle from t = 0 to $t = \frac{\pi}{6}$ as a definite d. integral and find this distance correct to three decimal places.

2 marks

$$d = \int_0^{\frac{\pi}{8}} |\chi(t)| dt = \int_0^{\frac{\pi}{8}} \sqrt{4\cos^2(xt) + 9\sin^2(xt)} dt$$

d ≈ 1.80 4: metres



b.

Question 2 (11 marks)

Two complex numbers, u and v, are defined as u = -2 - i and v = -4 - 3i.

Express the relation |z-u|=|z-v| in the cartesian form y=mx+c, where $m, c \in R$. a.

3 marks

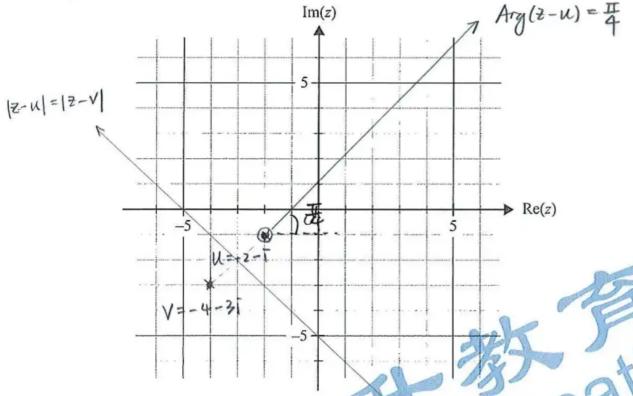
Square both sides & expandi

$$x^{2}+4x+y^{2}+3y+5=x^{2}+8x+y^{2}+6y+2f$$

We for $y: y=-x-5$



Plot the points that represent u and v and the relation |z - u| = |z - v| on the Argand diagram



2 marks

State a geometrical interpretation of the graph of |z-u| = |z-v| in relation to the points that c. represent u and v.

1 mark

Arg (2+2+1) = 4

1 mark

2020 SPECMATH EXAM 2

Write down the function that describes the ray $Arg(z-u) = \frac{\pi}{4}$, giving the rule in cartesian form.

Sketch the ray given by $Arg(z-u) = \frac{\pi}{4}$ on the Argand diagram in part b.

Cationark

d.

$$y+1=x+2$$

$$y=x+1$$

$$y:(-2,\infty)\to \mathbb{R}, y+(x)=x+1$$

The points representing u and v and -5i lie on the circle given by $|z-z_c|=r$, where z_c is the centre of the circle and r is the radius.

Find z_c in the form a + ib, where $a, b \in R$, and find the radius r.

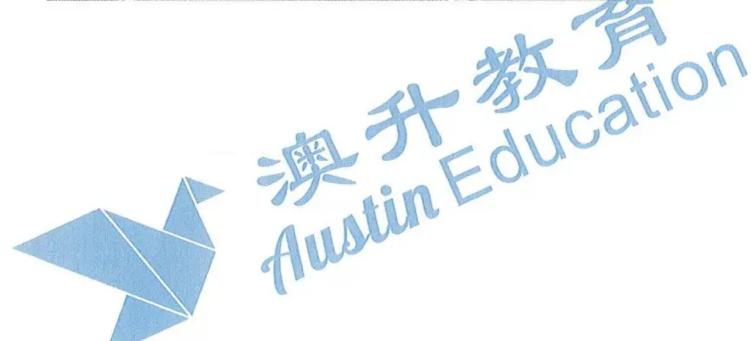
let the equ of circle be
$$(x-h)^2 + (y-k)^2 = \Gamma^2$$

Substitute $(-2,-1)$, $(-4,-3)$, $(0,-5)$:

$$\begin{cases} h^{2}+4h+k^{2}+2k+5=\Gamma^{2} & \text{Solve Shem for } h,k,\Gamma \\ h^{2}+8h+k^{2}+6k+2J=\Gamma^{2} & \text{where } \Gamma>0 \\ h^{2}+(k+5)^{2}=\Gamma^{2} & h=-\frac{5}{3}, k=\frac{-10}{3} \text{ and } \Gamma=\frac{5\sqrt{2}}{3} \end{cases}$$

Hence the equ of circle is
$$|z - (-\frac{1}{5} - \frac{1}{5}i)| = \frac{15}{5}$$

and $z_c = -\frac{1}{5} - \frac{15}{5}i$, $r = \frac{55}{5}$

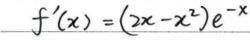


Question 3 (10 marks)

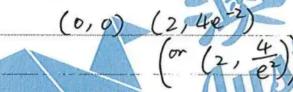
Let $f(x) = x^2 e^{-x}$.

a. Find an expression for f'(x) and state the coordinates of the stationary points of f(x).

2 marks



$$f'(x) = 0, e^{-x} \neq 0$$

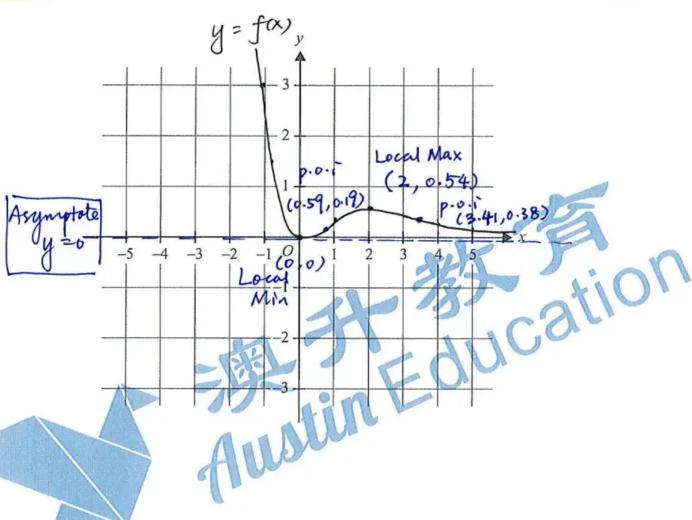


b. State the equation(s) of any asymptotes of f(x).

1 mark

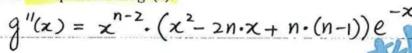
y=0, the only horizontal asymptote

c. Sketch the graph of y = f(x) on the axes provided below, labelling the local maximum stationary point and all points of inflection with their coordinates, correct to two decimal places.



Let $g(x) = x^n e^{-x}$, where $n \in \mathbb{Z}$.

d. Write down an expression for g''(x).



1 mark

e. i. Find the non-zero values of x for which g''(x) = 0.

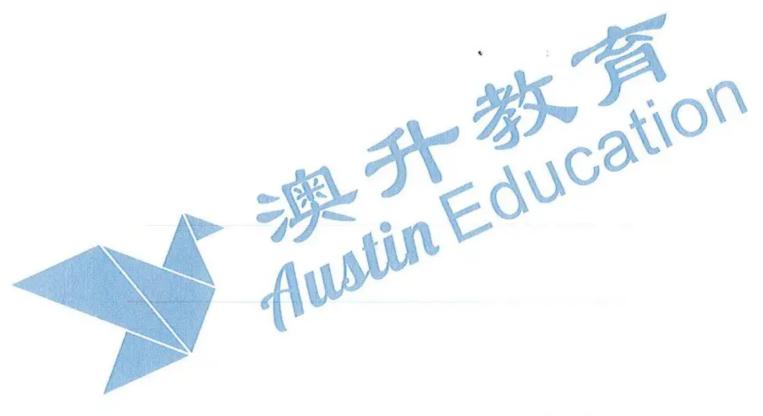
1 mark

$$x = n - \sqrt{n}$$
 or $x = n + \sqrt{n}$

where n + In + 0

ii. Complete the following table by stating the value(s) of n for which the graph of g(x) has the given number of points of inflection.

Number of points of inflection	Value(s) of n (where $n \in \mathbb{Z}$)	
0	n e Z U {0}	
1	$\gamma = 1$	
2	n = 2,4,6,8,zk	,(k>1 and k ∈ Z)
3	n=3,5,7,9,,2	k+1, (K>1, and K+ T).



Question 4 (14 marks)

A pilot is performing at an air show. The position of her aeroplane at time t relative to a fixed origin

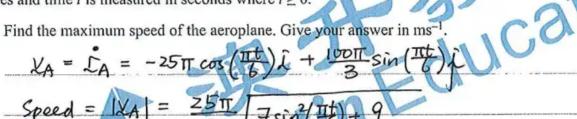
O is given by $\underline{\underline{r}}_{A}(t) = \left(450 - 150\sin\left(\frac{\pi t}{6}\right)\right)\underline{\underline{i}} + \left(400 - 200\cos\left(\frac{\pi t}{6}\right)\right)\underline{\underline{j}}$, where $\underline{\underline{i}}$ is a unit vector in a

horizontal direction, j is a unit vector vertically up, displacement components are measured in metres and time t is measured in seconds where $t \ge 0$.

Find the maximum speed of the aeroplane. Give your answer in ms

3 marks

2 marks



Consider the bornel properties of sin (76):

$$= \left(\frac{100}{3}\Pi\right)m/s$$

No need !

i. Use $r_A(t)$ to show that the cartesian equation of the path of the aeroplane is given by b.

 $\frac{(x-450)^2}{22500} + \frac{(y-400)^2}{40000} = 1.$

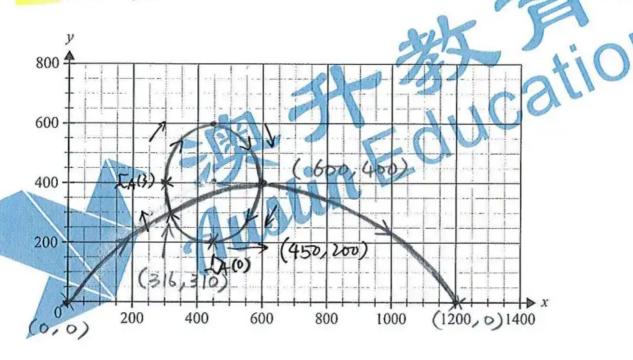
$$x = 450 - 150 \sin\left(\frac{\pi t}{6}\right)$$

$$\frac{x-450}{-150} = \sin\left(\frac{\pi t}{6}\right)$$

$$\frac{\left(x-450\right)^2}{23120} = \sin^2\left(\frac{\pi t}{6}\right)$$

Sketch the path of the aeroplane on the axes provided below. Label the position of the aeroplane when t = 0, using coordinates, and use an arrow to show the direction of motion of the aeroplane.

3 marks



A friend of the pilot launches an experimental jet-powered drone to take photographs of the air show. The position of the drone at time t relative to the fixed origin is given by

 $\underline{\mathbf{r}}_{\mathbf{D}}(t) = (30t)\underline{\mathbf{i}} + (-t^2 + 40t)\underline{\mathbf{j}}$, where t is in seconds and $0 \le t \le 40$, $\underline{\mathbf{i}}$ is a unit vector in the same horizontal direction, j is a unit vector vertically up, and displacement components are measured in metres.

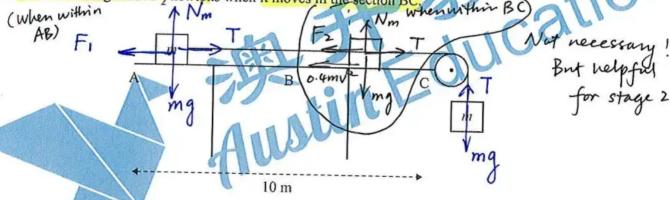
Sketch the path of the drone on the axes provided in part b.ii. Using coordinates, label the c. points where the path of the drone crosses the path of the aeroplane, correct to the nearest metre.

Solve
$$\begin{cases} x = 30t \\ y = -t^2 + 40t \end{cases}$$
, $t, y \end{cases}$ $y = \frac{-x(x - 1200)}{900}$
Then solve with the ellipse $(31b, 310)$ & $(b00, 400)$



Question 5 (13 marks)

Two objects, each of mass m kilograms, are connected by a light inextensible string that passes over a smooth pulley, as shown below. The object on the platform is initially at point A and, when it is released, it moves towards point C. The distance from point A to point C is 10 m. The platform has a rough surface and, when it moves along the platform, the object experiences a horizontal force opposing the motion of magnitude F_1 newtons in the section AB and a horizontal force opposing the motion of magnitude F_2 newtons when it moves in the section BC.



a. On the diagram above, mark all forces that act on each object once the object on the platform has been released and the system is in motion.

Do we need both stages?

2 marks

The force F_1 is given by $F_1 = kmg$, $k \in \mathbb{R}^+$.

b. i. Show that an expression for the acceleration, in ms⁻², of the object on the platform, in terms of k, as it moves from point A to point B is given by $\frac{g(1-k)}{2}$.

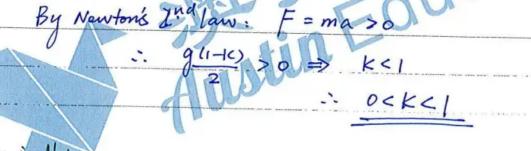
2 marks

Over AB: Fret =
$$(m+m)a = mg - T + T - F$$
,
 $\Rightarrow 2ma = mg - kmg$
 $\Rightarrow 2ma = mg(I-k)$
 $\Rightarrow 2a = g(I-k)$
 $\Rightarrow a = g(I-k)$

ii. The system will only be in motion for certain values of k.

Find these values of k.

1 mark



strategically embedded y!

AC = 10m AB = 5m

c. Find, in terms of k, the time taken, in seconds, for the object on the platform to reach point B. 2 marks

u=0, x=5, a=2(1-1c)	
$5 = 4 (2(1-k)) \times t^2, t \ge 0$	The state of
$t = 2 \frac{5}{5}$ for 10	P. etc)
VgCI-K) (7V	1-K

d. Express, in terms of k, the speed v_B , in ms⁻¹, of the object on the platform when it reaches point B.

 $V = \sqrt{5} \times \sqrt{\frac{9}{9(1-k)}} \times \sqrt{\frac{5}{9(1-k)}}$ with g = 9.8 $V = \sqrt{5} \times \sqrt{\frac{9}{9(1-k)}} = \sqrt{5} \frac{9}{9(1-k)} = \sqrt{5} \frac{1}{9(1-k)} = \sqrt{5} \frac{1}{9($

e. When the object on the platform is at point B, the string breaks. The velocity of the object at point B is $v_B = 2.5 \text{ ms}^{-1}$. The force that opposes motion from point B to point C is $F_2 = 0.075 \text{ mg} + 0.4 \text{ mv}^2$, where v is the velocity of the object when it is a distance of x metres from point B. The object on the platform comes to rest before point C.

Find the object's distance from point C when it comes to rest. Give your answer in metres, correct to two decimal places.

4 marks

The new equ of motion is
$$F = ma = -(0.075 mg + 0.4 mv^2)$$

$$\therefore a = -(0.075 g + 0.4 v^2)$$

$$\begin{cases} x = 0, v = 2.5 & v \frac{dv}{dx} = -(0.075 g + 0.4 v^2) \end{cases}$$

 $\begin{cases} x = d, \ V = V_{stop} = 0 \Rightarrow \int_{0.075g + 0.4V^2}^{0.075g + 0.4V^2} dV = \int_{0.075g + 0.4V^2}^{0.075g + 0.4V^2} dV = 0$

d = 5 loge (647) m

= 5- 5 loge (647) = 5- 5 loge (147)

N=57 N=0