

Student Name: \_\_\_\_\_

## MATHEMATICAL METHODS (CAS)

### Units 3 & 4 – Written examination 1



### 2008 Trial Examination

Reading time: 15 minutes

Writing time: 1 hour

### QUESTION AND ANSWER BOOK

#### Structure of book

<i>Number of questions</i>	<i>Number of questions to be answered</i>	<i>Number of marks</i>
12	12	40
		Total 40

- Students are permitted to bring into the examination room: pens, pencils, highlighters, erasers, sharpeners and rulers
- Students are NOT permitted to bring into the examination room: blank sheets of paper and/or white out liquid/tape.
- No calculator is permitted in this examination.

#### Materials supplied

- Question and answer book of 10 pages.

#### Instructions

- Print your name in the space provided on the top of this page.
- All written responses must be in English.

**Students are NOT permitted to bring mobile phones and/or any other unauthorised electronic communication devices into the examination room.**

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**Instructions**

Answer **all** questions in the spaces provided.

A decimal approximation will not be accepted if an **exact** answer is required to a question.

In questions where more than one mark is available, appropriate working must be shown.

Unless otherwise indicated, the diagrams in this book are **not** drawn to scale.

**Question 1**

- a. State the transformations made to the graph of  $y = \frac{1}{x}$  in order to obtain the graph

$$y = -\frac{4}{x-3} - 2.$$

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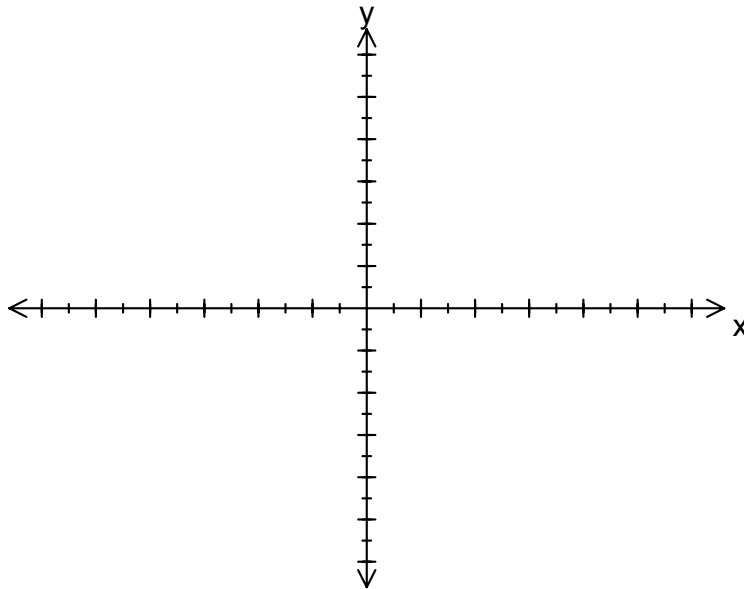
1 mark

- b. Hence or otherwise, sketch  $y = -\frac{4}{x-3} - 2$  and label any asymptote(s) and axial intercept(s).

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3 marks

**TURN OVER**

**Question 2**

Solve  $2^{2x} - 2^{x+3} + 2^4 = 0$ .

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3 marks

**Question 3**

a. If  $f(x) = 1 - 2e^{x-1}$ , find the inverse function  $f^{-1}(x)$ .

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3 marks

b. State the domain and range of  $f^{-1}(x)$ .

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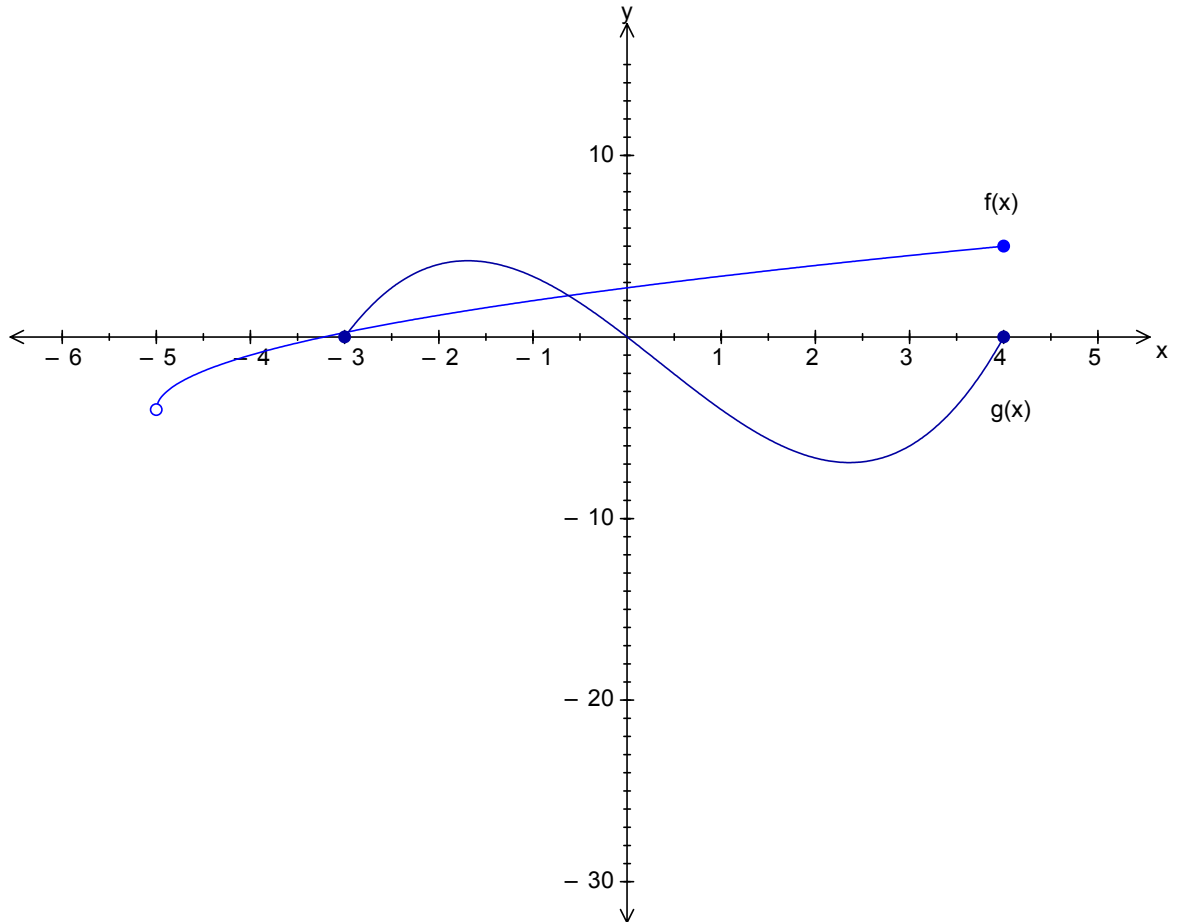
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1 mark

**Question 4**

Two functions are defined as:  $f : (-5,4] \rightarrow R, f(x) = 3\sqrt{x+5} - 4$  and

$g : [-3,4] \rightarrow R, g(x) = \frac{x}{3}(x+3)(x-4)$ . The graphs of these functions are shown below.



a. On the same set of axes, sketch the graph of  $h(x) = f(x).g(x)$ .

2 marks

b. State the domain of  $h(x)$ .

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1 mark

**TURN OVER**

**Question 5**

a. If  $f(x) = \frac{(3x^2 - 2)^4}{\cos(x)}$ , find  $f'(x)$ .

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1 mark

b. Find the derivative of  $y = x^2 e^{2x}$ .

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1 mark

c. Hence find  $\int (xe^{2x} + x^2 e^{2x} + 1) dx$ .

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1 mark

**Question 6**

Solve the equation  $\sqrt{3} \sin(3x) = \cos(3x)$  for  $x \in [-\pi, \pi]$ .

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3 marks

**Question 7**

- a. Sketch the graph of  $y = 2 \tan\left(\frac{1}{2}\left(x - \frac{\pi}{2}\right)\right)$  for  $x \in \left(-\frac{\pi}{2}, \frac{7\pi}{2}\right)$ . Label the coordinates of all axial intercepts.

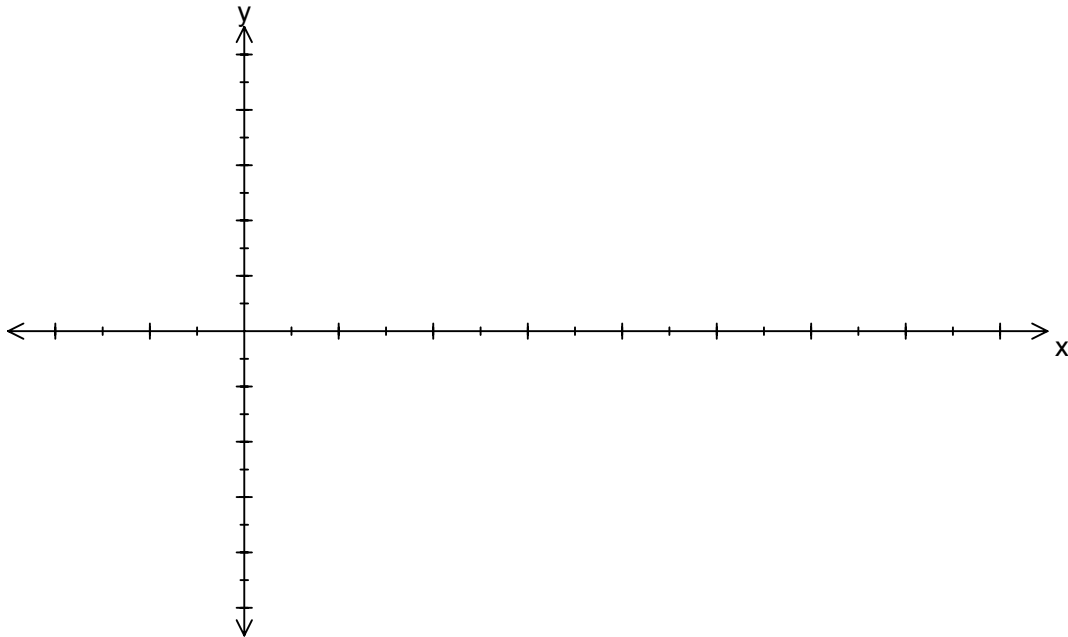
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3 marks

- b. On the same set of axes, sketch  $y = \left| 2 \tan\left(\frac{1}{2}\left(x - \frac{\pi}{2}\right)\right) \right|$  for  $x \in \left(-\frac{\pi}{2}, \frac{7\pi}{2}\right)$ .

1 mark

**TURN OVER**

**Question 8**

Find the equation of the tangent to the curve  $y = 3\ln(2x - 3)$  at the point where  $x = 3$

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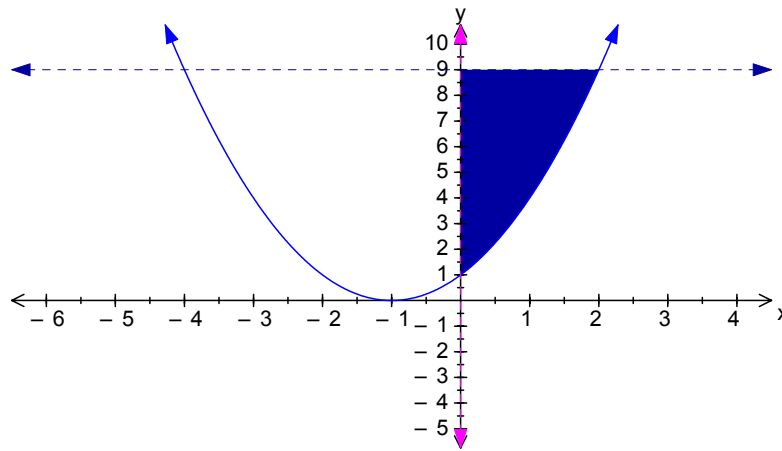


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3 marks

**Question 9**

Find the area between the graph of  $y = (x + 1)^2$ , the right of the **y axis** and the line  $y = 9$




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3 marks



**Question 10**

A discrete probability distribution is given by the following table

$x$	0	1	2	3	4
$p(x)$	0.2	$a$	$b$	0.2	0.2

- a. If  $E(X) = 2.1$ , find the values of  $a$  and  $b$ .

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2 marks

- b. Find  $E(2X + 1)$ .

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1 mark

**TURN OVER**

**Question 11**

Tests have shown that if a cat has milk on a particular day, there's a 90% chance that it will choose pellets on the next day. But if a cat has pellets on a particular day, there is an 80% chance that it will choose milk on the next day.

- a. If Jim's cat had milk on Monday, find the probability that it will have pellets on Thursday. Give answer as a **fraction**.

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4 marks

**Question 12**

The heights of women are normally distributed with a mean of 160cm and a standard deviation of 8cm.

- a. Between what values are approximately 95% of the women's heights?

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1 mark

- b. If  $\Pr(H > 170) = 0.1$ , then find the probability that a woman's height is less than 170cm, given that it is more than 160cm.

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2 marks

**END OF QUESTION AND ANSWER BOOK**