

# 2011

## VCE

### Further Mathematics

### Trial Examination 2



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### **PURPOSE OF THIS TRIAL EXAMINATION**

This Further Mathematics Trial Examination is designed to assess

- understanding and communication of mathematical ideas
- interpretation, analysis and solution of routine problems
- interpretation, analysis and solution of non-routine problems

Assessment is by extended answer questions involving multi-stage solutions of increasing complexity.

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# **FURTHER MATHEMATICS**

## **Written examinations 1 and 2**

### **FORMULA SHEET**

#### **Directions to students**

Detach this formula sheet during reading time.

This formula sheet is provided for your reference.

**Further Mathematics Formulas****Core: Data analysis**

standardised score: 
$$z = \frac{x - \bar{x}}{s_x}$$

least squares line: 
$$y = a + bx \text{ where } b = r \frac{s_y}{s_x} \text{ and } a = \bar{y} - b\bar{x}$$

residual value: 
$$\text{residual value} = \text{actual value} - \text{predicted value}$$

seasonal index: 
$$\text{seasonal index} = \frac{\text{actual figure}}{\text{deseasonalised figure}}$$

**Module 1: Number patterns**

arithmetic series: 
$$a + (a + d) + \dots + (a + (n - 1)d) = \frac{n}{2}[2a + (n - 1)d] = \frac{n}{2}(a + l)$$

geometric series: 
$$a + ar + ar^2 + \dots + ar^{n-1} = \frac{a(1 - r^n)}{1 - r}, r \neq 1$$

infinite geometric series: 
$$a + ar + ar^2 + ar^3 + \dots = \frac{a}{1 - r}, |r| < 1$$

**Module 2: Geometry and trigonometry**

area of a triangle: 
$$\frac{1}{2}bc \sin A$$

Heron's formula: 
$$A = \sqrt{s(s - a)(s - b)(s - c)} \text{ where } s = \frac{1}{2}(a + b + c)$$

circumference of a circle: 
$$2\pi r$$

area of a circle: 
$$\pi r^2$$

volume of a sphere: 
$$\frac{4}{3}\pi r^3$$

surface area of a sphere: 
$$4\pi r^2$$

volume of a cone: 
$$\frac{1}{3}\pi r^2 h$$

volume of a cylinder: 
$$\pi r^2 h$$

volume of a prism: 
$$\text{area of base} \times \text{height}$$

volume of a pyramid: 
$$\frac{1}{3} \text{area of base} \times \text{height}$$

Pythagoras' theorem:  $c^2 = a^2 + b^2$

sine rule:  $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

cosine rule:  $c^2 = a^2 + b^2 - 2ab \cos C$

### Module 3: Graphs and relations

#### Straight line graphs

gradient (slope):  $m = \frac{y_2 - y_1}{x_2 - x_1}$

equation:  $y = mx + c$

### Module 4: Business-related mathematics

simple interest:  $I = \frac{\text{Pr}T}{100}$

compound interest:  $A = PR^n$  where  $R = 1 + \frac{r}{100}$

hire purchase: effective rate of interest  $\approx \frac{2n}{n+1} \times \text{flat rate}$

annuities:  $A = PR^n - \frac{Q(R^n - 1)}{R - 1}$ , where  $R = 1 + \frac{r}{100}$

### Module 5: Networks and decision mathematics

Euler's formula:  $v + f = e + 2$

### Module 6: Matrices

determinant of a  $2 \times 2$  matrix:  $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ ;  $\det A = \begin{vmatrix} a & b \\ c & d \end{vmatrix} = ad - bc$

inverse of a  $2 \times 2$  matrix:  $A^{-1} = \frac{1}{\det A} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$  where  $\det A \neq 0$

**END OF FORMULA SHEET**

**Specific Instructions**

This task paper consists a core and six modules. Students should answer **all** questions in the core and then select **three** modules and answer **all** questions within the modules selected.

	<b>Page</b>
<b>Core:</b> Data analysis	2
<b>Module</b>	
Module 1: Number patterns and applications .....	8
Module 2: Geometry and trigonometry .....	13
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Module 5: Networks and decision mathematics .....	28
Module 6: Matrices .....	34

**Core: Data analysis****Question 1**

Day	Melbourne		Sydney	
	Max Temp °C	Evaporation mm	Max Temp °C	Evaporation mm
1	19.5	1.2	27.7	7.8
2	19.8	3.6	27.7	6.0
3	20.1	4.6	27.3	6.4
4	18.6	5.0	27.2	5.5
5	24.5	3.4	26.5	4.8
6	28.0	4.8	22.4	3.1
7	29.2	7.2	25.0	5.7
8	27.2	10.8	28.2	7.2
9	23.8	2.6	37.8	10.9
10	18.7	1.8	25.5	4.2
11	27.1	0.6	26.4	7.5
12	30.7	9.2	30.0	8.6
13	22.4	6.8	29.8	8.5
14	24.5	7.1	35.4	10.2

The above table shows the maximum temperatures in °C and the amount of evaporation in millimeters for Melbourne and Sydney over a two - week period.

- a. For Melbourne's maximum temperature over this period what is the mean and standard deviation? Give your answers to one decimal place.

---

1 mark

- b. What percentage of Melbourne's maximum temperatures was above its mean maximum temperature during this period?

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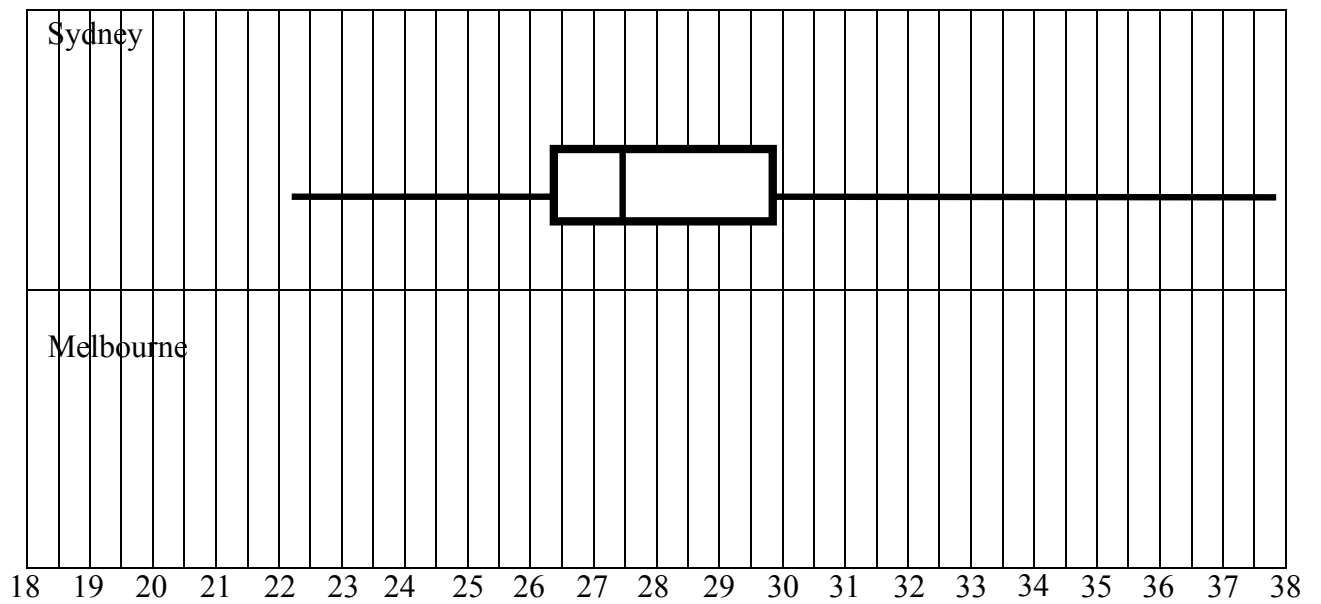
1 mark



**Core: Data analysis**

**Question 1 (continued)**

- c. In the space provided, draw the box plot for the maximum temperatures for Melbourne for this period.



2 marks

- d. What is the interquartile range for Melbourne's maximum temperatures for this period?

\_\_\_\_\_

1 mark

- e. Describe what the box plots show with regard to temperatures in the two cities.

\_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_

1 mark

**Core: Data analysis****Question 2**

- a. Complete the following stem and leaf graph for Melbourne's evaporation over this two – week period.

0	
1	2 8
2	6
3	4 6
4	6 8
5	0
6	8
7	1 2
8	
9	2
10	0 8

1 mark

- b. What is the median evaporation of Melbourne over this time?

---

1 mark

- c. Are there any outliers for Melbourne's evaporation over this time. Give reasons.

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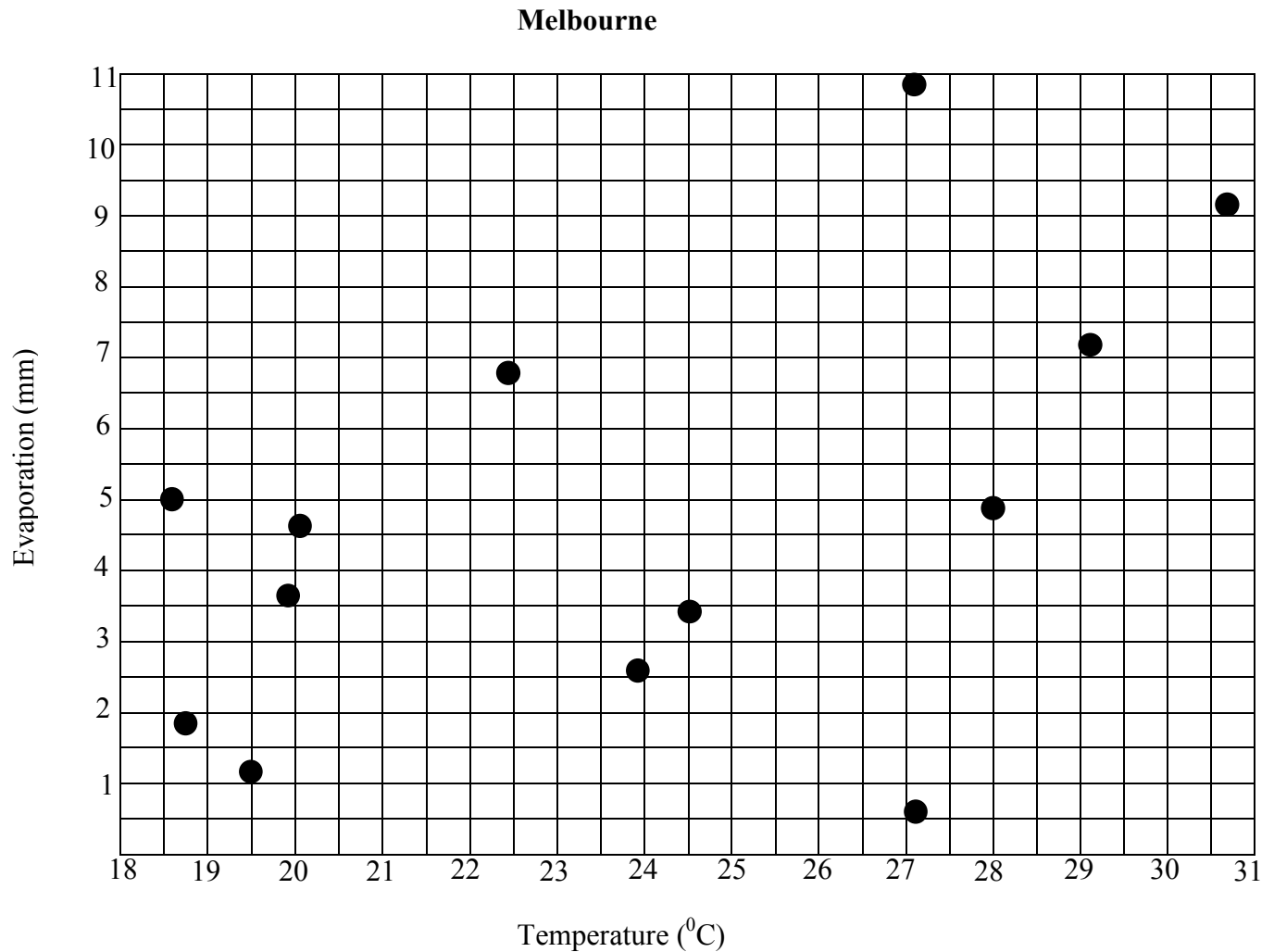
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1 mark

**Core: Data analysis****Question 3**

The scatter plot below shows the evaporation and maximum temperature for Melbourne for the given fourteen days.



- a. On the above scatter plot mark the point corresponding to the 14<sup>th</sup> day with an **X**.

1 mark

- b. What is the equation of the least squares regression line? Give your answer in terms of temperature and evaporation. Give all numbers to one decimal place.

1 mark

**Core: Data analysis****Question 3 (continued)**

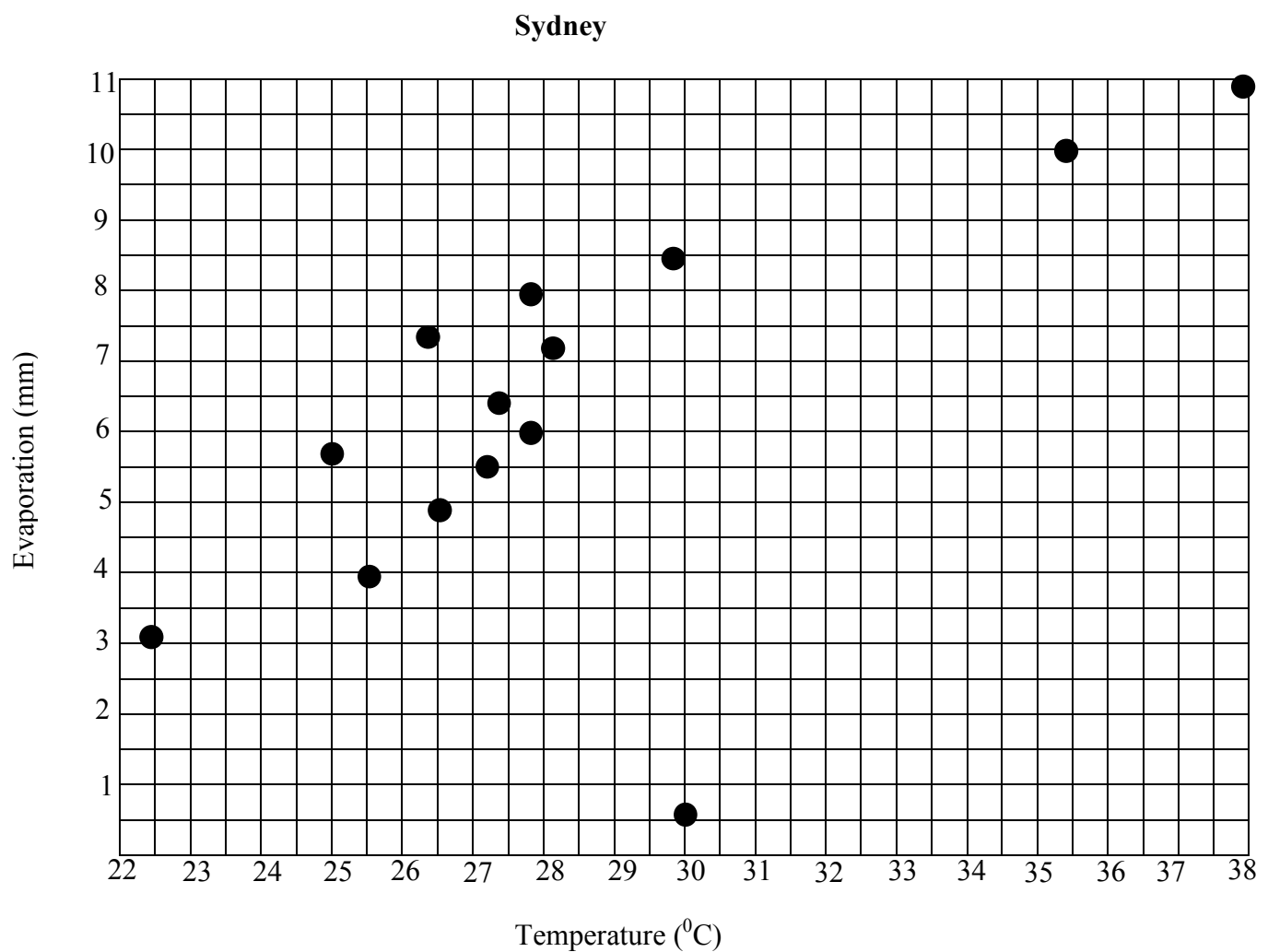
- c. What is the strength of the linear relationship? Support your answer by using the appropriate statistic.

---

1 mark

**Question 4**

The scatter plot below shows the evaporation and maximum temperature for Sydney for the given fourteen days.



**Core: Data analysis****Question 4 (continued)**

- a. What are the coordinates of the two points used to determine the gradient of the three median line?

---

1 mark

- b. What is the gradient of this line? Give your answer to one decimal place.

---

1 mark

- c. From the three median line, by how many millimeters would you predict that the evaporation would increase for each additional  $0.5^{\circ}\text{C}$  increase in temperature?

---

1 mark

**Total = 15 marks****End of Core: Data analysis**

**Module 1 : Number patterns and applications**

If you choose this module, all questions are to be answered.

**Question 1**

Bess checks her emails every 20 minutes, starting at 9.00 am and notes the following pattern

Checking time	Number of new emails
9.00 am	2
9.20 am	5
9.40 am	8

If this pattern continues

**a. i.** How many new emails will she receive at 10.00 am?

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1 mark

**a. ii.** How many new emails will she have when she checks her emails for the seventh time?

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1 mark

**a. iii.** At what time will Bess check her emails for the seventh time?

---

1 mark

**Module 1: Number patterns and applications**

**Question 1 (continued)**

**a. iv.** At what time will Bess find 41 new emails on her computer?

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2 marks

**a. v.** How many emails will Bess have received between 9.00am and 2.00 pm inclusive?

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1 mark

**Module 1: Number patterns and applications****Question 2**

Bess responds to her emails every 20 minutes, starting at 9.20 am. She notes that the number of new emails she responds to follows a pattern.

Time responses start	Number of new emails responded to
9.20 am	1
9.40 am	2
10.00 am	4

If this pattern continues

**a. i.** How many emails will Bess respond to at 10.20 am?

---

1 mark

**a. ii.** Of all the emails that will have come in by 9.40, how many will remain unanswered after Bess has done her 9.40 replies?

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1 mark

**a. iii.** How many emails altogether will Bess have answered after she has answered her emails at 10.40 am?

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1 mark

**a. iv.** How many emails will remain unanswered after Bess has answered her emails at 10.40 am?

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1 mark



**Module 1: Number patterns and applications****Question 2 (continued)**

- a. v.** What is the earliest time that Bess will not have sufficient emails to answer and so will be unable to continue the pattern of responses?

---

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---

1 mark

**Question 3**

At 10.40 am, Bess decides to change the pattern she is using to answer her emails so that the number of emails she and her assistants respond to from 10.40 on is given by the equation

$$E_n = 2E_{n-1} - a \quad E_1 = 16$$

**a.**

- i.** What value of  $a$  would make the number of emails that Bess and her assistants respond to, in each 20 minute time slot, a constant?

---

1 mark

**b.** If  $a = 4$

- i.** Find  $E_2$

---

1 mark

- ii.** If from 11.30 am on, Bess and her assistants receive a total of 500 emails every 20 minutes, and the number of emails that they reply to at 12.20 pm is 388, find the number of emails that they replied to at midday.

---

1 mark

**Module 1: Number patterns and applications****Question 3 (continued)**

- c. Each day, the number of emails that Bess receives satisfies the difference equation  $T_n = 0.1T_{n-1}$ . If she receives  $p$  emails on the first day, then how many emails in terms of  $p$  will she receive in the long run?

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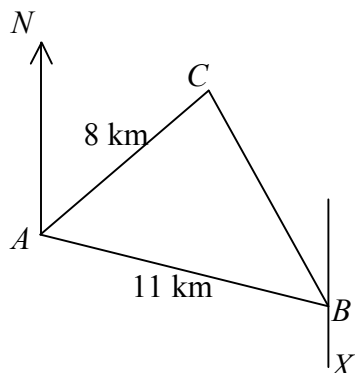
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1 mark

**Total = 15 marks****End of Module 1: Number patterns and applications**

**Module 2: Geometry and trigonometry**

If you choose this module, all questions are to be answered.

**Question 1**

The buoy,  $B$ , is on a bearing of  $120^\circ$  from the port,  $A$ . Chris sails 8 km from the port,  $A$ , on a bearing of  $048^\circ$  to the buoy,  $C$ .  $N$  is due north of  $A$  and  $X$  is due south of  $B$ .

- a. What is the magnitude of  $\angle NAC$  ?

---

1 mark

- b. Find  $\angle CAB$ .

---

1 mark

- c. Find the distance between the two buoys,  $B$  and  $C$ .  
Give your answer to two decimal places.

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1 mark

**Module 2: Geometry and trigonometry**

**Question 1 (continued)**

**d.** Find angle  $ABX$ .

---

1 mark

**e.** Find the bearing of  $C$  from  $B$ . Give your answer to the nearest degree.

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1 mark

**f.** How far north of  $B$  is  $C$ ? Give your answer to the nearest kilometre.

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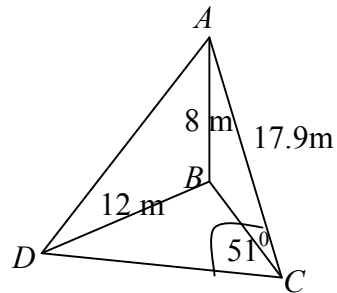
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1 mark

**Module 2: Geometry and trigonometry****Question 2**

At the harbour there is a restaurant with an outdoor floor area,  $BCD$ . A sailcloth stretches from  $A$  which is directly above  $B$  to  $CD$ .  $AB = 8$  m,  $BD = 12$  m,  $AC = 17.9$  m and  $\angle ACD = 51^\circ$ ,



- a. Find  $AD$ , giving your answer to one decimal place.

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1 mark

- b. Show that  $\angle DAC = 54^\circ$  to the nearest degree.

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1 mark

- c. How much material had to be purchased to make the sailcloth?  
Give your answer to the nearest square metre.

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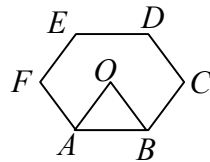
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1 mark

**Module 2: Geometry and trigonometry****Question 3**

There is a play area for children at the restaurant. One of the pieces of play equipment is an hexagonal prism with a cylinder cut through the centre for children to crawl through.

- a. Before the cylinder was cut from the hexagonal prism, the top of the prism was a regular hexagon of side length 1.5 m.



- i. Find  $\angle AOB$  where O is the centre of the hexagonal face,  $ABCDEF$ .

---

1 mark

- ii. What is the area of the hexagonal face,  $ABCDEF$ ?  
Give your answer to two decimal places.

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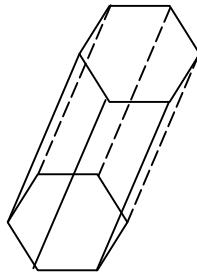
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1 mark

**Module 2: Geometry and trigonometry****Question 3 (continued)****b.**

If the hexagonal prism has a height of 2 m. what is the surface area of the prism before the cylinder has been cut out? Give your answer to two decimal places.

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1 mark

**c.** A cylinder is cut through the centre of the hexagonal prism to allow space for the children to crawl through. If the base of the cylinder has a diameter of 1 m.

**i.** What area on the top of the hexagonal prism remains?  
Give your answer to two decimal places.

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---

1 mark

**ii.** What is the area of the curved surface of the cylinder?  
Give your answer to one decimal place.

---

1 mark

**Module 2: Geometry and trigonometry**

**Question 3 (continued)**

**c.**

- iii.** What is the total surface area of this piece of play equipment?  
Give your answer to the nearest whole number.

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1 mark

**Total 15 marks**

**End of Module 2: Geometry and trigonometry**

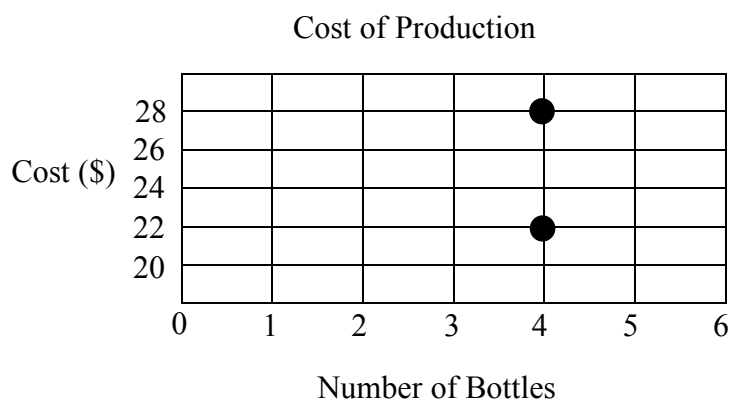


**Module 3: Graphs and relations**

If you choose this module, all questions are to be answered.

**Question 1**

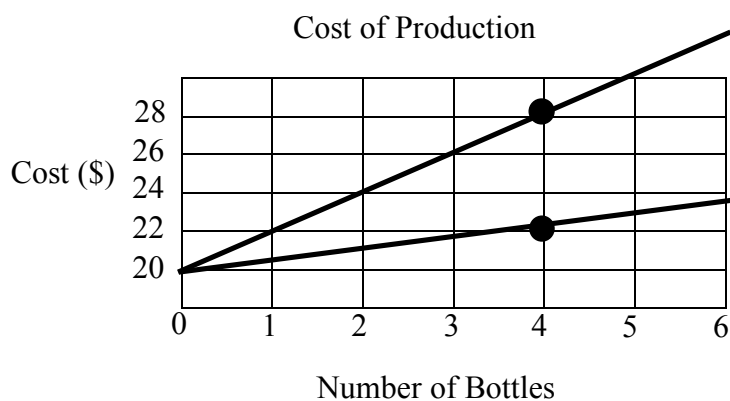
The Kleen Hair Company produces shampoo and conditioner where a bottle of shampoo costs more to produce than a bottle of conditioner. The production manager shows the cost of producing four bottles of each type of hair product on the graph below.



- a. How much did four bottles of shampoo cost?

---

1 mark



The company produces the above graph for their products.

- b. i. What does the point (0,20) on both lines mean?

---

1 mark

**Module 3: Graphs and relations****Question 1 (continued)**

**b. ii.** Write the equation for the cost of producing  $x$  bottles of shampoo.

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1 mark

**b. iii.** If the Kleen Hair company makes 100 bottles of shampoo and 100 bottles of conditioner in one batch, what would be the cost of production of a batch?

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1 mark

**b. iv.** In another batch, the company spends \$517 making shampoo and conditioner. If the company spent \$73 on the conditioner made in this batch, what was the total number of bottles of shampoo and conditioner made in this batch?

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2 marks

**Module 3: Graphs and relations****Question 2**

The Kleen Hair Company produces 10,000 bottles of shampoo in a day and sells the shampoo for \$20 a bottle.

- a. What would be the revenue from selling  $x$  bottles of shampoo?

---

1 mark

- b. How much would it cost the Kleen Hair Company to produce 10,000 bottles of shampoo?

---

1 mark

- c. What would be the minimum number of bottles of shampoo that the Kleen Hair Company would have to sell each day in order not to make a loss for that day?

---

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1 mark

**Module 3: Graphs and relations****Question 3**

The Smith family is going on an overseas holiday and Mrs. Smith wants to take a supply of the family's favourite shampoo and conditioner. She can buy the shampoo on special for \$15 a bottle, while the conditioner costs \$10 a bottle. Mrs. Smith wants to buy at least two bottles of shampoo and no more than three bottles of conditioner and she does not want to spend more than \$150. In addition, she wants to spend at least twice as much on shampoo as she spends on conditioner. She buys  $x$  bottles of shampoo and  $y$  bottles of conditioner.

- a. Write down an inequation involving  $x$  and  $y$  and the \$150 that Mrs. Smith can spend.

---

1 mark

Three of the other four inequalities are listed below

$$y \geq 0$$

$$y \leq 3$$

$$15x \geq 20y \Rightarrow 3x \geq 4y$$

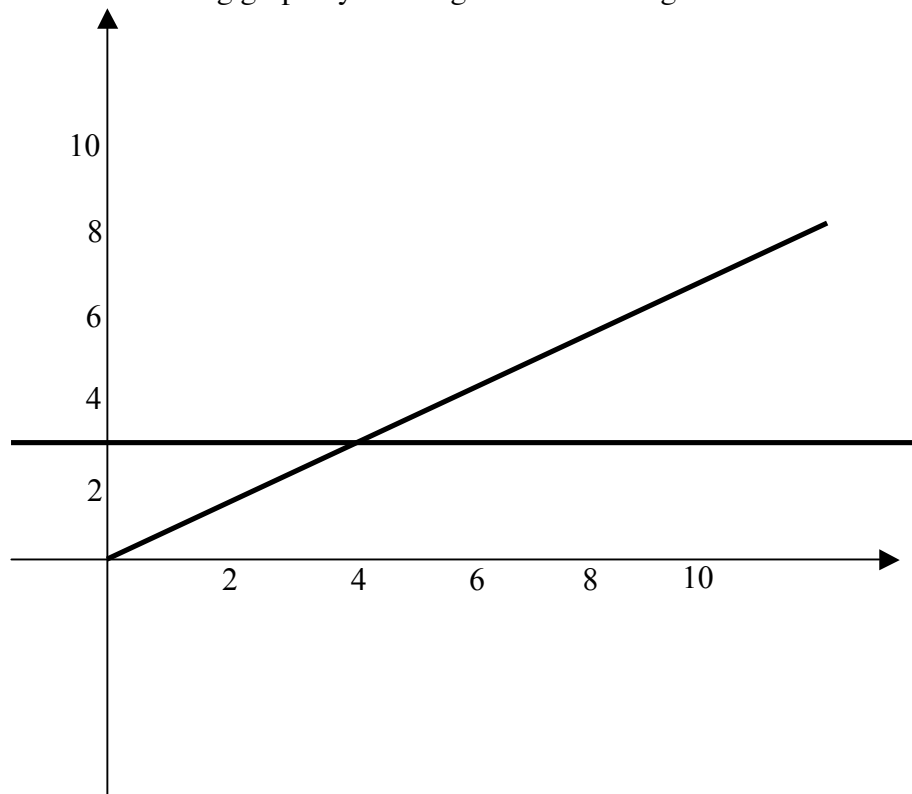
- b. Write down the remaining inequality.

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1 mark

**Module 3: Graphs and relations****Question 3 (continued)**

- c. Complete the following graph by drawing the two missing lines.



2 marks

- d. On the above graph, shade the region that satisfies all the constraints.

1 mark

- e. What is the maximum number of bottles of shampoo and conditioner that Mrs. Smith can buy?

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1 mark

**Total = 15 marks****End of Module 3: Graphs and relations**

**Module 4: Business-related mathematics**

If you choose this module, all questions are to be answered.

**Question 1**

Paul and Polly own a small business and have bank accounts with different banks. Their monthly bank statement for one of these banks is shown below. The interest paid on this account is 4% per annum based on the minimum monthly balance.

Date	Details	Withdrawals	Deposits	Balance
1 June	Opening Balance			\$2825.07
11 June	EFTPOS	204		
15 June	Deposit		6000	
23 June	ATM withdrawal			8441.07
28 June	Deposit		8000	
29 June	Phone banking transfer of funds	13000		
30 June	Interest for month of June			

Paul spilt his glass of water over the statement and some of the entries are illegible.

- a. What was the minimum monthly balance for the month of June?

---



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1 mark

- b. How much money was withdrawn on the 23<sup>rd</sup> of June?

---

1 mark

- c. What was the interest rate for the month of June? Give your answer to two decimal places.

---

1 mark

**Module 4: Business-related mathematics****Question 1 (continued)**

- d. How much interest was paid into this account for the month of June? Give your answer to the nearest cent.

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---

1 mark

- e. What will the opening balance be for 1<sup>st</sup> July if no transactions are carried out that day by either Paul or Poppy?

---

1 mark

**Question 2**

- a. Paul and Polly need transport for their business. Paul suggests that they purchase a new truck valued at \$39000 on hire purchase. They have savings of \$10000 that they can use as a deposit and they would then have to pay a monthly instalment of \$652.50 for 5 years.

- i. How much will they actually pay for this car?

---

1 mark

- ii. How much interest will they pay?

---

- iii. What is the interest rate per annum?

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1 mark

1 mark

**Module 4: Business-related mathematics****Question 2 (continued)**

- b.** Polly says that she has seen a suitable second hand truck for \$15000 at the car yard in the next suburb. She says that they could use their \$10000 savings and borrow the remainder of the money at 6% per annum compounded monthly for five years. She said that they would not have to repay any money until the end of the five years.
- i.** How much money would they owe at the end of the five-year period if they made no repayments during this time? Give your answer to the nearest cent.

---

1 mark

- ii.** If they repaid \$100 a month how much would they owe at the end of the 5 year period? Give your answer to the nearest cent.

---

1 mark

- iii.** If they repaid \$652.50 a month how long would it take to repay the loan?

---

1 mark



**Module 4: Business-related mathematics****Question 3**

- a. The new truck that Paul chooses depreciates at 20% per annum on a reducing value. What will the book value of this truck be at the end of five years? Give your answer to the nearest dollar.

---

---

1 mark

- b. The second hand truck that Polly chooses depreciates at a flat rate of \$4.40 for every 100 km travelled. If the truck is expected to do 30,000 km per year, what will be the book value of this truck at the end of five years?

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---

1 mark

- c. What would the percentage depreciation per annum of Paul's truck need to be for both trucks to have the same book value at the end of the 5 years? Give your answer to one decimal place.

---

1 mark

- d. By how much would the flat rate depreciation for every 100 km travelled by Polly's truck need to change so that Polly's truck would have the same book value as Paul's truck at the end of 5 years?

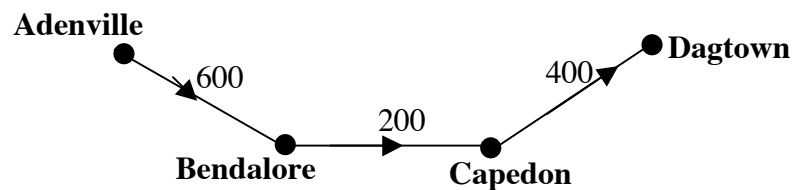
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1 mark

**Total = 15 marks****End of Module 4: Business-related mathematics**

**Module 5: Networks and decision mathematics**

If you choose this module, all questions are to be answered.

**Question 1**

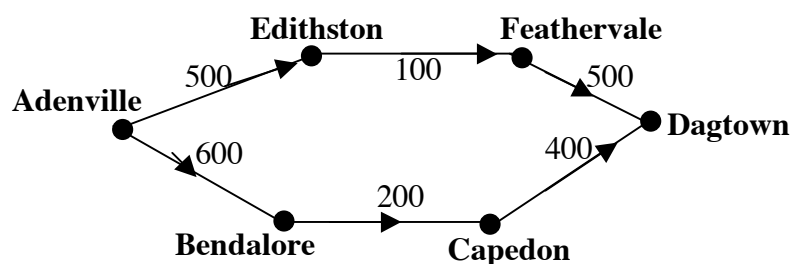
The above diagram shows the roads connecting four towns, Adenville, Bendalore, Capedon and Dagtown. The numbers on the graph show the number of vehicles that can travel along each section of road per hour.

- a. What is the maximum number of cars that can travel from Adenville to Dagtown per hour?

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1 mark

The council adds more roads joining Adenville to Dagtown via Edithston and Feathervale.



- b. What is the maximum number of cars that can now travel from Adenville to Dagtown per hour?

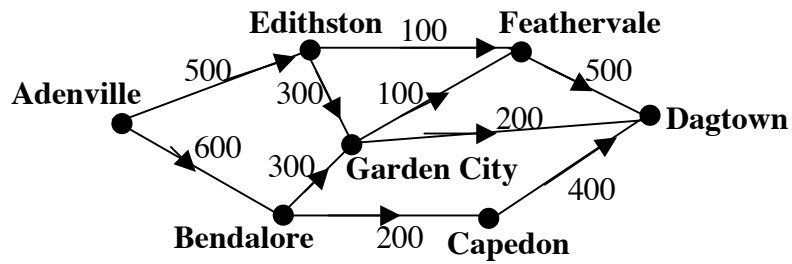
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1 mark

**Module 5: Networks and decision mathematics**

**Question 1 (continued)**

- c. The council adds even more roads going through the town of Garden City.



- i. What is the maximum number of cars that can now travel from Adenville to Dagtown per hour?

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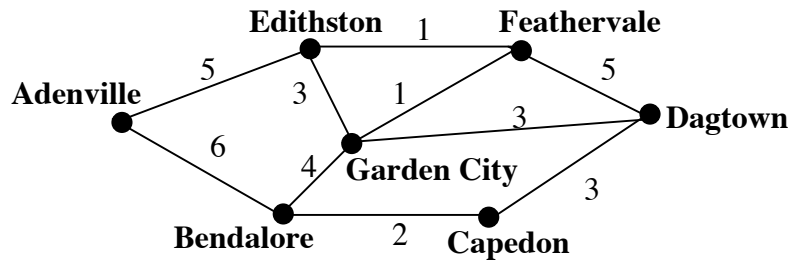
1 mark

- ii. Mark the minimum cut on the above graph.

1 mark

**Module 5: Networks and decision mathematics****Question 1 (continued)**

d.



The above graph shows the distances in kilometers between the seven towns. A telephone company wants to install new telephone wire to connect each of the above towns. The wires are to be laid above the roads required to connect all the towns. What would be the shortest length of wire required?

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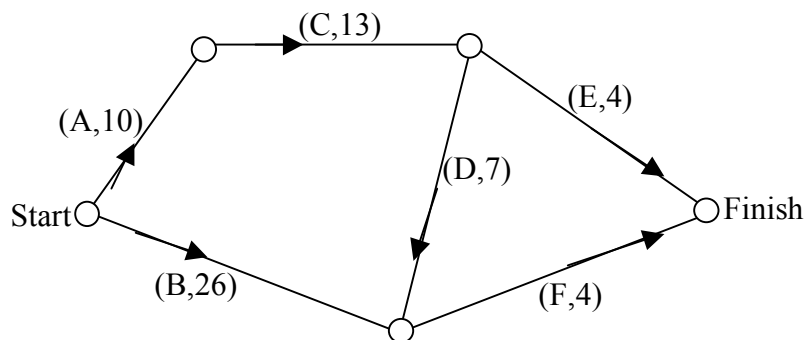


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1 mark

**Module 5: Networks and decision mathematics****Question 2**

Mr. Wong runs a manufacturing business in Dagtown. The following network shows the different activities that must be carried out in order to complete a single manufacturing item, the activities that must be completed before certain activities can start and the time in days for the completion of each activity.



- a. Which activity must be completed before activity C can start?

---

1 mark

- b. Which activity does **not** have to be completed before activity F starts?

---

1 mark

- c. What is the critical path?

---

1 mark

**Module 5: Networks and decision mathematics****Question 2 (continued)**

- d.** What is the minimum time it will take for Mr. Wong to complete a single manufacturing item?

---

1 mark

- e.** What is the earliest time that activity F can commence?

---

1 mark

- f.** What is the float time for activity E?

---

1 mark

- g.** If activity E were delayed by another 10 hours,

- i.** How would this affect the completion time?

---

---

1 mark

- ii.** What would the latest start time now be for activity F

---

1 mark

**Module 5: Networks and decision mathematics****Question 2 (continued)**

- h.** Assume there had been no extra delay in completing activity E and that the total cost of the manufacturing process for one item was \$300 per day. Mr. Wong hires an extra person at \$350 per day to help out with activity A. This extra person halves the completion time for activity A. How much would Mr. Wong save on the whole project, or how much extra would the whole project now cost him?

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2 marks

**Total = 15 marks****End of Module 5: Networks and decision mathematics**





**Module 6: Matrices**

**Question 1 (continued)**

c. If  $B = A \times S$  what information would matrix  $B$  provide?

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---

1 mark

**Module 6: Matrices****Question 2**

In a round robin five tennis teams, the Anchors, Bull Dogs, Condors, Dragons and Emus played each other. Some of the results were as follows

The Anchors defeated the Bull Dogs.  
The Condors defeated the Anchors, Bull Dogs and Dragons.  
The Dragons defeated the Anchors and Bull Dogs.

In order to rank the teams the following dominance matrix,  $D$ , was set up using all the results of the round robin

$$D = \begin{matrix} & \begin{matrix} A & B & C & D & E \end{matrix} \\ \begin{matrix} A \\ B \\ C \\ D \\ E \end{matrix} & \begin{bmatrix} 0 & 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 1 & 0 & 1 & 0 \\ y & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 \end{bmatrix} \end{matrix}$$

- a. Explain the meaning of 0 and 1 in the above matrix.

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1 mark

- b. What is the value of  $y$ ?

---

1 mark

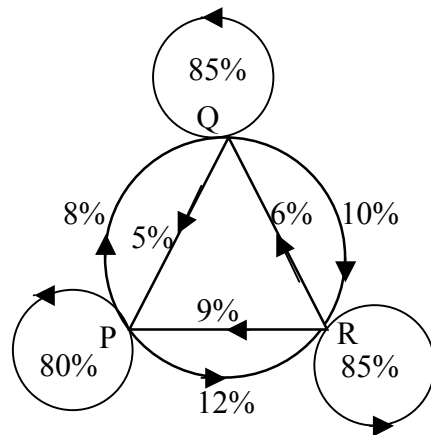
- c. Who defeated the Emus?

---

1 mark

**Module 6: Matrices****Question 3**

There are three tennis centres in a certain town, Physical, Quality and Rigour. It has been noted that on 1<sup>st</sup>. January 2010, Physical had 50% of the market, while Quality and Rigour had 25% each.



The above diagram shows the movement of members from one tennis centre to another each year.

- a. What percentage of members remains with Physical each year?

---

1 mark

- b. What percentage of members move from Rigour to Physical each year?

---

1 mark

**Module 6: Matrices****Question 3 (continued)**

- c. Complete the transition matrix that can be used to represent the information in the diagram.

$$\begin{array}{c}
 \text{To} \\
 P \\
 Q \\
 R
 \end{array}
 \begin{bmatrix}
 & P & Q & R \\
 P & & 0.05 & \\
 Q & 0.08 & & \\
 R & & & 0.85
 \end{bmatrix}
 \begin{array}{c}
 \text{From} \\
 P \\
 Q \\
 R
 \end{array}$$

1 mark

- d. If there are 800 members altogether in the three tennis centres, what is the column matrix,  $N$ , that shows the number of members at each tennis centre on 1<sup>st</sup> January 2010?

---

 1 mark

- e. How many members would you expect to belong to the Physical tennis centre on 1<sup>st</sup>. January 2011?

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 1 mark

**Module 6: Matrices****Question 3 (continued)**

- f. How many more members would Rigour have on 1<sup>st</sup>. January 2011 than it had on 1<sup>st</sup>. January 2010?

---

1 mark

- g. How many members would you expect Quality to have on 1<sup>st</sup>. January 2015?

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1 mark

- h. In the long term, which sports centre will have the least number of members?

---

1 mark

- i. How many members can Rigour expect to have in the long term?

---

1 mark

**Total = 15 marks****End of Module 6: Matrices****END OF QUESTION AND ANSWER BOOK  
2011 Further Mathematics Trial Examination 2**

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